

2.3: Introduction to Forlan

The Forlan toolset is implemented as a set of Standard ML (SML) modules. It's used interactively. In fact, a Forlan session is nothing more than a Standard ML session in which the Forlan modules are available.

Instructions for installing and running Forlan on machines running Linux, macOS and Windows can be found on the Forlan website: <https://alleystoughton.us/forlan/>.

We begin this section by giving a quick introduction to SML.

We then show how symbols, strings, finite sets of symbols and strings, and finite relations on symbols can be manipulated using Forlan.

Invoking Forlan

To invoke Forlan, type the command `forlan` to your shell (command processor):

```
% forlan
Forlan Version m (based on Standard ML of New Jersey
Version n)
val it = () : unit
-
```

SML's prompt is “-”. To exit SML, type *CTRL-d* under Linux and macOS, and *CTRL-z* under Windows. To interrupt back to the SML top-level, type *CTRL-c*.

Invoking Forlan (Cont.)

On Windows, you may find it more convenient to invoke Forlan by double-clicking on the Forlan icon.

Actually, a much more flexible and satisfying way of running Forlan is as a subprocess of the Emacs text editor. See the Forlan website for information about how to do this.

Evaluating Expressions

The simplest way of using SML is as a calculator:

```
- 4 + 5;  
val it = 9 : int  
- it * it;  
val it = 81 : int  
- it - 1;  
val it = 80 : int  
- 5 div 2;  
val it = 2 : int  
- 5 mod 2;  
val it = 1 : int  
- ~4 + 2;  
val it = ~2 : int
```

SML responds to each expression by printing its value and type (`int` is the type of integers), and noting that the expression's value has been bound to the identifier `it`. Expressions must be terminated with semicolons. Negative numbers begin with `~`.

More Types

In addition to the type `int` of integers, SML has types `string` and `bool`, product types $t_1 * \dots * t_n$, and list types `t list`.

```
- "hello" ^ " " ^ "there";
val it = "hello there" : string
- not true;
val it = false : bool
- true andalso (false orelse true);
val it = true : bool
- if 5 < 7 then "hello" else "bye";
val it = "hello" : string
- (3 + 1, 4 = 4, "a" ^ "b");
val it = (4,true,"ab") : int * bool * string
- [1, 3, 5] @ [7, 9, 11];
val it = [1,3,5,7,9,11] : int list
- rev it;
val it = [11,9,7,5,3,1] : int list
- length it;
val it = 6 : int
```

More Types (Cont.)

```
- null[];  
val it = true : bool  
- null[1, 2];  
val it = false : bool  
- hd[1, 2, 3];  
val it = 1 : int  
- tl[1, 2, 3];  
val it = [2,3] : int list
```

More Types (Cont.)

It also has option types `t option`:

```
- NONE;  
val it = NONE : 'a option  
- SOME 3;  
val it = SOME 3 : int option  
- SOME true;  
val it = SOME true : bool option
```

`NONE` is an example of a *polymorphic* value. It has all of the types that can be formed by instantiating the type variable `'a` with a type: `int option`, `bool option`, etc.

Value Declarations

In SML, it is possible to bind the value of an expression to an identifier using a value declaration:

```
- val x = 3 + 4;  
val x = 7 : int  
- val y = x + 1;  
val y = 8 : int
```


Value Declarations

In SML, it is possible to bind the value of an expression to an identifier using a value declaration:

```
- val x = 3 + 4;  
val x = 7 : int  
- val y = x + 1;  
val y = 8 : int
```

One can even give names to the components of a tuple, or give a name to the data of a non-**NONE** optional value:

```
- val (x, y, z) = (3 + 1, 4 = 4, "a" ^ "b");  
val x = 4 : int  
val y = true : bool  
val z = "ab" : string  
- val SOME n = SOME(4 * 25);  
val n = 100 : int
```

Let Expressions

One can use a `let` expression to carry out some declarations in a local environment, evaluate an expression in that environment, and yield the result of that evaluation:

```
- val x = 3;
val x = 3 : int
- val z = 10;
val z = 10 : int
- let val x = 4 * 5
=      val y = x * z
= in (x, y, x + y) end;
val it = (20,200,220) : int * int * int
- x;
val it = 3 : int
```

When a declaration or expression spans more than one line, SML prints its secondary prompt, `=`, on all of the lines except for the first one. SML doesn't process a declaration or expression until it is terminated with a semicolon.

Function Declarations

One can declare functions, and apply those functions to arguments:

```
- fun f n = n + 1;
val f = fn : int -> int
- f(4 + 5);
val it = 10 : int
- fun g(x, y) = (x ^ y, y ^ x);
val g = fn : string * string -> string * string
- val (u, v) = g("a", "b");
val u = "ab" : string
val v = "ba" : string
```

The function `f` maps its input `n` to its output `n + 1`. All function values are printed as `fn`. A type `t1 -> t2` is the type of all functions taking arguments of type `t1` and producing results of type `t2`. Note that SML infers the types of functions, and that the type operator `*` has higher precedence than the operator `->`.

Anonymous Functions

Forlan has *anonymous* functions, which may also be given names using value declarations:

```
- (fn x => x + 1)(3 + 4);  
val it = 8 : int  
- val f = fn x => x + 1;  
val f = fn : int -> int  
- f(3 + 4);  
val it = 8 : int
```

Functions as Data

Functions are data: they may be passed to functions, returned from functions (a function that returns a function is called *curried*), be components of tuples or lists, etc. For example,

```
val map : ('a -> 'b) -> 'a list -> 'b list
```

is a polymorphic, curried function. The type operator `->` associates to the right, so that `map`'s type is

```
val map : ('a -> 'b) -> ('a list -> 'b list)
```

`map` takes in a function f of type `'a -> 'b`, and returns a function that when called with a list of elements of type `'a`, transforms each element using f , forming a list of elements of type `'b`.

Functions as Data (Cont.)

```
- val f = map(fn x => x + 1);  
val f = fn : int list -> int list  
- f[2, 4, 6];  
val it = [3,5,7] : int list  
- f[~2, ~1, 0];  
val it = [~1,0,1] : int list  
- map (fn x => x mod 2 = 1) [3, 4, 5, 6, 7];  
val it = [true,false,true,false,true] : bool list
```

In the last use of `map`, we are using the fact that function application associates to the left, so that $f \times y$ means $(f x)y$, i.e., apply f to x , and then apply the resulting function to y .

Recursive Functions

It's also possible to declare recursive functions, like the factorial function:

```
- fun fact n =  
=       if n = 0  
=       then 1  
=       else n * fact(n - 1);  
val fact = fn : int -> int  
- fact 4;  
val it = 24 : int
```

Loading the Contents of Files

One can load the contents of a file into SML using the function

```
val use : string -> unit
```

The type `unit` has the single element `()`. For example, if the file `fact.sml` contains the declaration of the factorial function, then this declaration can be loaded into the system as follows:

```
- use "fact.sml";  
[opening fact.sml]  
val fact = fn : int -> int  
val it = () : unit  
- fact 4;  
val it = 24 : int
```


Pattern Matching

We can define functions using pattern matching. E.g., we could (inefficiently) define the list reversal function like this:

```
- fun rev nil          = nil
=   | rev (x :: xs) = rev xs @ [x];
val rev = fn : 'a list -> 'a list
```

Calling `rev` with the empty list (`[]` or `nil`) will result in the empty list being returned. And calling it with a nonempty list will temporarily bind `x` to the list's head, bind `xs` to its tail, and then evaluate the expression `rev xs @ [x]`, making a recursive call to `rev xs`, and then returning the result of appending the result of this call and `[x]`. The official definition of `rev` is more efficient; see the book.

Recursive Datatypes

We can define recursive datatypes, and define functions by structural recursion on recursive datatypes. E.g., here's how we can define the datatype of labeled binary trees:

```
- datatype ('a, 'b) tree =  
=   Leaf of 'b  
=   | Node of 'a * ('a, 'b) tree * ('a, 'b) tree;  
datatype ('a, 'b) tree  
  = Leaf of 'b  
  | Node of 'a * ('a, 'b) tree * ('a, 'b) tree  
- Leaf;  
val it = fn : 'a -> ('b, 'a) tree  
- Node;  
val it = fn  
  : 'a * ('a, 'b) tree * ('a, 'b) tree -> ('a, 'b) tree
```

Recursive Datatypes (Cont.)

```
- val tr =  
=       Node(true,  
=         Node(false, Leaf 7, Leaf ~1),  
=         Leaf 8);  
val tr =  
  Node (true,Node (false,Leaf 7,Leaf ~1),Leaf 8)  
  : (bool,int) tree
```

Recursive Datatypes (Cont.)

Then we can define a function for reversing a tree, and apply it to `tr`:

```
- fun revTree (Leaf n)                = Leaf n
=   | revTree (Node(m, tr1, tr2)) =
=       Node(m, revTree tr2, revTree tr1);
val revTree = fn : ('a,'b) tree -> ('a,'b) tree
- revTree tr;
val it =
  Node (true,Leaf 8,Node (false,Leaf ~1,Leaf 7))
  : (bool,int) tree
- revTree it;
val it =
  Node (true,Node (false,Leaf 7,Leaf ~1),Leaf 8)
  : (bool,int) tree
```

Symbols

The Forlan module `Sym` defines the abstract type `sym` of symbols, as well as some functions for processing symbols, including:

```
val input  : string -> sym
val output : string * sym -> unit
val equal  : sym * sym -> bool
```

These functions behave as follows:

- `input fil` reads a symbol from file `fil`; if `fil = ""`, then the symbol is read from the standard input;
- `output(fil, a)` writes the symbol `a` to the file `fil`; if `fil = ""`, then the string is written to the standard output;
- `equal` tests whether two symbols are equal.

Symbols (Cont.)

The type `sym` is bound in the top-level environment; on the other hand, one must write `Sym.f` to select the function `f` of module `Sym`.
Whitespace characters are ignored by Forlan's input routines.
Interactive input is terminated by a line consisting of a single `."` (dot, period). Forlan's prompt is `@`.

Symbols (Cont.)

The module `Sym` also provides the functions

```
val fromString : string -> sym
val toString   : sym -> string
```

where

- `fromString` is like `input`, except that it takes its input from a string;
- `toString` is like `output`, except that it writes its output to a string.

In the future, whenever a module/type has `input` and `output` functions, you may assume that it also has `fromString` and `toString` functions.

Symbols (Cont.)

Here are some example uses of the functions of `Sym`:

```
- val a = Sym.input "";
@ <i
@ d>
@ .
val a = - : sym
- val b = Sym.fromString "<num>";
val b = - : sym
- Sym.output("", a);
<id>
val it = () : unit
- Sym.equal(a, b);
val it = false : bool
- Sym.equal(a, Sym.fromString "<id>");
val it = true : bool
```


Sets

The module `Set` defines the abstract type

```
type 'a set
```

of finite sets of elements of type `'a`. It is bound in the top-level environment. E.g., `sym set` is the type of sets of symbols. `Set` also provides various constants and functions for processing sets, but we will only make direct use of a few of them:

```
val toList   : 'a set -> 'a list
val size     : 'a set -> int
val empty    : 'a set
val isEmpty  : 'a set -> bool
val sing     : 'a -> 'a set
```

These values are polymorphic: `'a` can be `int`, `sym`, etc. The function `sing` makes a value `x` into the singleton set `{x}`.

Sets

More functions:

```
val filter : ('a -> bool) -> 'a set -> 'a set
val all    : ('a -> bool) -> 'a set -> bool
val exists : ('a -> bool) -> 'a set -> bool
```

`filter` keeps selected elements of a set, `all` tests whether all elements of a set satisfy a predicate, and `exists` tests whether at least one element of a set satisfies a predicate.

Sets of Symbols

The module `SymSet` defines various functions for processing finite sets of symbols (alphabets), including:

```
val input      : string -> sym set
val output     : string * sym set -> unit
val fromList   : sym list -> sym set
val memb       : sym * sym set -> bool
val subset     : sym set * sym set -> bool
val equal      : sym set * sym set -> bool
val union      : sym set * sym set -> sym set
val inter      : sym set * sym set -> sym set
val minus      : sym set * sym set -> sym set
val genUnion   : sym set list -> sym set
val genInter   : sym set list -> sym set
```

Sets of symbols are expressed in Forlan as sequences of symbols, separated by commas.

Sets of Symbols (Cont.)

Here are some example uses of the functions of `SymSet`:

```
- val bs = SymSet.input "";
@ a, <id>, 0, <num>
@ .
val bs = - : sym set
- SymSet.output("", bs);
0, a, <id>, <num>
val it = () : unit
- val cs = SymSet.input "";
@ a, <char>
@ .
val cs = - : sym set
- SymSet.subset(cs, bs);
val it = false : bool
- val ds = SymSet.fromString "<char>, <>";
val ds = - : sym set
```

Sets of Symbols (Cont.)

More examples:

```
- SymSet.output("", SymSet.union(bs, cs));  
0, a, <id>, <num>, <char>  
val it = () : unit  
- SymSet.output("", SymSet.inter(bs, cs));  
a  
val it = () : unit  
- SymSet.output("", SymSet.minus(bs, cs));  
0, <id>, <num>  
val it = () : unit  
- SymSet.output("", SymSet.genUnion[bs, cs, ds]);  
0, a, <>, <id>, <num>, <char>  
val it = () : unit  
- SymSet.output("", SymSet.genInter[bs, cs, ds]);  
  
val it = () : unit
```

Strings

We will be working with two kinds of strings:

- SML strings, i.e., elements of type `string`;
- The strings of formal language theory, which we call “formal language strings”, when necessary.

The module `Str` defines the type `str` of formal language strings, which is bound in the top-level environment, and is equal to `sym list`, the type of lists of symbols.

Because strings are lists, we can use SML’s list processing functions on them.

Strings are expressed in Forlan’s input syntax as either a single `%` or a nonempty sequence of symbols.

Strings (Cont.)

The module `Str` defines some functions for processing strings, including:

```
val input      : string -> str
val output     : string * str -> unit
val alphabet  : str -> sym set
val equal     : str * str -> bool
val prefix    : str * str -> bool
val suffix    : str * str -> bool
val substr    : str * str -> bool
val power     : str * int -> str
val last      : str -> sym
val allButLast : str -> str
```

Strings (Cont.)

Here are some example uses of the functions of `Str`:

```
- val x = Str.input "";
@ hello<there>
@ .
val x = [-,-,-,-,-] : str
- length x;
val it = 6 : int
- Str.output("", x);
hello<there>
val it = () : unit
- SymSet.output("", Str.alphabet x);
e, h, l, o, <there>
val it = () : unit
- Str.output("", Str.power(x, 3));
hello<there>hello<there>hello<there>
val it = () : unit
```


Strings (Cont.)

```
- val y = Str.fromString "ello";  
val y = [-,-,-,-] : str  
- Str.equal(y, x);  
val it = false : bool  
- Str.prefix(y, x);  
val it = false : bool  
- Str.substr(y, x);  
val it = true : bool  
- val z = Str.fromString "h" @ y;  
val z = [-,-,-,-,-] : sym list  
- Str.prefix(z, x);  
val it = true : bool
```

Strings (Cont.)

```
- val x = Str.fromString "hellothere";  
val x = [-,-,-,-,-,-,-,-,-] : str  
- null x;  
val it = false : bool  
- Sym.output("", hd x);  
h  
val it = () : unit  
- Str.output("", tl x);  
ellothere  
val it = () : unit  
- Sym.output("", Str.last x);  
e  
val it = () : unit  
- Str.output("", Str.allButLast x);  
hellother  
val it = () : unit
```

Sets of Strings

The module `StrSet` defines various functions for processing finite sets of strings, including:

```
val input      : string -> str set
val output    : string * str set -> unit
val fromList  : str list -> str set
val memb      : str * str set -> bool
val subset    : str set * str set -> bool
val equal     : str set * str set -> bool
val union     : str set * str set -> str set
val inter     : str set * str set -> str set
val minus     : str set * str set -> str set
val genUnion  : str set list -> str set
val genInter  : str set list -> str set
val alphabet  : str set -> sym set
```

Sets of strings are expressed in Forlan as sequences of strings, separated by commas.

Sets of Strings (Cont.)

Here are some example uses of the functions of `StrSet`:

```
- val xs = StrSet.input "";
@ hello, <id><num>, %
@ .
val xs = - : str set
- val ys = StrSet.input "";
@ <id><num>, another
@ .
val ys = - : str set
- val zs = StrSet.union(xs, ys);
val zs = - : str set
- Set.size zs;
val it = 4 : int
- StrSet.output("", zs);
%, <id><num>, hello, another
val it = () : unit
```

Sets of Strings (Cont.)

More examples:

```
- val us = Set.filter (fn x => length x mod 2 = 0) zs;  
val us = - : sym list set  
- StrSet.output("", us);  
%, <id><num>  
val it = () : unit  
- SymSet.output("", StrSet.alphabet zs);  
a, e, h, l, n, o, r, t, <id>, <num>  
val it = () : unit
```

Relations on Symbols

The module `SymRel` defines the type `sym_rel` of finite relations on symbols. It is bound in the top-level environment, and is equal to `(sym * sym)set`, i.e., its elements are finite sets of pairs of symbols.

`SymRel` also defines various functions for processing finite relations on symbols, including:

```
val input      : string -> sym_rel
val output    : string * sym_rel -> unit
val fromList  : (sym * sym)list -> sym_rel
val memb      : (sym * sym) * sym_rel -> bool
val subset    : sym_rel * sym_rel -> bool
val equal     : sym_rel * sym_rel -> bool
```

Relations on symbols are expressed in Forlan as sequences of ordered pairs (a, b) of symbols, separated by commas.

Relations on Symbols (Cont.)

More functions:

```
val union      : sym_rel * sym_rel -> sym_rel
val inter     : sym_rel * sym_rel -> sym_rel
val minus     : sym_rel * sym_rel -> sym_rel
val genUnion  : sym_rel list -> sym_rel
val genInter  : sym_rel list -> sym_rel
```

Relations on Symbols (Cont.)

More functions:

```
val domain      : sym_rel -> sym set
val range       : sym_rel -> sym set
val reflexive   : sym_rel * sym set -> bool
val symmetric   : sym_rel -> bool
val transitive  : sym_rel -> bool
val function    : sym_rel -> bool
val applyFunction : sym_rel -> sym -> sym
```


Relations on Symbols (Cont.)

More functions:

```
val domain      : sym_rel -> sym set
val range       : sym_rel -> sym set
val reflexive   : sym_rel * sym set -> bool
val symmetric   : sym_rel -> bool
val transitive  : sym_rel -> bool
val function    : sym_rel -> bool
val applyFunction : sym_rel -> sym -> sym
```

`reflexive(rel, bs)` tests whether *rel* is reflexive on *bs*.

Relations on Symbols (Cont.)

More functions:

```
val domain      : sym_rel -> sym set
val range       : sym_rel -> sym set
val reflexive   : sym_rel * sym set -> bool
val symmetric   : sym_rel -> bool
val transitive  : sym_rel -> bool
val function    : sym_rel -> bool
val applyFunction : sym_rel -> sym -> sym
```

`reflexive(rel, bs)` tests whether *rel* is reflexive on *bs*.

The function `applyFunction` is *curried*. Given a relation *rel*, it checks that *rel* is a function, issuing an error message, otherwise. If *rel* is a function, it returns a function of type `sym -> sym` that, when called with a symbol *a*, will apply the function *rel* to *a*.

Relations on Symbols (Cont.)

Here are some example uses of the functions of `SymRel`:

```
- val rel = SymRel.input "";  
@ (1, 2), (2, 3), (3, 4), (4, 5)  
@ .  
val rel = - : sym_rel  
- SymSet.output("", SymRel.domain rel);  
1, 2, 3, 4  
val it = () : unit  
- SymSet.output("", SymRel.range rel);  
2, 3, 4, 5  
val it = () : unit
```

Relations on Symbols (Cont.)

More examples:

```
- SymRel.reflexive(rel, SymSet.fromString "1, 2");  
val it = false : bool  
- SymRel.symmetric rel;  
val it = false : bool  
- SymRel.transitive rel;  
val it = false : bool  
- SymRel.function rel;  
val it = true : bool
```

Relations on Symbols (Cont.)

More examples:

```
- val f = SymRel.applyFunction rel;
val f = fn : sym -> sym
- Sym.output("", f(Sym.fromString "3"));
4
val it = () : unit
- Sym.output("", f(Sym.fromString "4"));
5
val it = () : unit
- Sym.output("", f(Sym.fromString "5"));
argument not in domain

uncaught exception Error
-
```